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## High Frequency Transformer Design and Optimization using Bio-inspired Algorithms

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### ABSTRACT

High frequency (HF) transformer at the isolation stage of SST plays a vital role in deciding the power conversion efficiency of the SST system. This paper proposes a new design procedure for optimization of HF transformer used in SST applications such that it fulfils all the requirements pertaining to its operating conditions. The novel design procedure proposed is based on optimizing the core geometry (in 5th power of cm), which has direct influence on regulation and copper loss. An isolated half-bridge DC–DC converter topology is chosen for implementing the proposed design. Four bio-inspired algorithms, namely Particle swarm optimization (PSO), Whale Optimization algorithm (WOA), Dragonfly Algorithm (DA), and Ant Lion Optimizer (ALO) are used to solve the optimization problem and the results are compared with Genetic algorithm (GA). Finally, the optimization results are validated through PowerEsim, a web-based testing platform with huge database of real-time components from leading manufacturers across the globe.

### Introduction

The evolution of Solid State Transformer (SST) in recent years as a promising new class of grid assets can be attributed to their ability to offer service extensions beyond voltage transformation, such as provision for dual power output (both dc and ac), input–output decoupling, high switching frequency, fault isolation, better power quality, etc. The heart of the SST system is the high frequency (HF) isolated dc–dc converter, which provides galvanic isolation between the medium voltage AC grid and a low voltage AC/DC grid as shown in [Figure 1.](#page-2-0) Though the choice of HF results in reduced footprint for the transformer, it also leads to higher switching losses and saturation of magnetic components. Further, the reduction in footprint entails an increased loss density in the transformer, which necessitates significant efforts on thermal management (Meier et al. [2009\)](#page-18-0). Thus a robust design procedure is required which collectively addresses the HF, isolation and

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<span id="page-2-0"></span>Figure 1. Basic three stage SST architecture.

thermal management issues and yields desired efficiency concurrently retaining the %regulation and power losses within specified limits.

<span id="page-2-13"></span><span id="page-2-8"></span><span id="page-2-3"></span>Numerous high/medium frequency transformer design solutions for various applications were established in literature. Earlier, researchers have attempted to develop detailed HF transformer design for switching power supplies (Coonrod [1986;](#page-17-0) McLyman Colonel [1993](#page-18-1); Pressman [1998](#page-19-0); Rama Rao et al. [2004\)](#page-19-1). The design considerations of medium frequency transformers for railway traction applications were discussed in literature in the previous decade (Kjellqvist, Norrga, and Ostlund [2004](#page-18-2); Steiner and Reinold [2007](#page-19-2)). The design optimization of high/medium frequency transformers for DC offshore applications was also documented in the past (Bahmani [2014](#page-17-1); Bahmani, Thiringer, and Kharezy [2015\)](#page-17-2). Research efforts on design of high/medium frequency transformers for SST applications have been widely reported in literature (Du et al. [2010;](#page-18-3) Huina, Xiaodong, and Gang [2012](#page-18-4); Ortiz et al. [2013;](#page-18-5) She et al. [2014](#page-19-3); Montoya, Mallela, and Balda [2015](#page-18-6)).

<span id="page-2-12"></span><span id="page-2-9"></span><span id="page-2-7"></span><span id="page-2-5"></span><span id="page-2-4"></span><span id="page-2-2"></span>Further, a thorough survey of literature reveals that research contribution toward HF transformer design have come in the way of optimizing the core based on area product (Farhangi and Akmal [1999](#page-18-7); McLyman [1993](#page-18-1)), optimizing the flux density of the core and current density of the windings (Petkov [1996](#page-19-4)), optimization including HF effects (Hurley, Wolfle, and Breslin [1998](#page-18-8)), optimization with arbitrary current and voltage waveforms (Breslin, [2002](#page-17-3)), high isolation requirements and thermal management (Ortiz, Biela, and Kolar [2010\)](#page-18-9), minimizing the losses taking leakage inductance and phase shifted angle of the converter into consideration (Hoang and Wang [2012](#page-18-10)), optimization with emphasis on thermal and insulation design (Peng and Jurgen [2013\)](#page-18-11) and maximizing the power density by accounting for tuned leakage inductance (Bahmani M.A. [2014](#page-17-1); Bahmani M.A. et al. [2015](#page-17-2)).

<span id="page-2-11"></span><span id="page-2-10"></span><span id="page-2-6"></span><span id="page-2-1"></span>All the aforementioned research efforts focus on either single or multiobjective optimization with or without single/multiple constraints with a procedure involving verification of bounds for parameter values other than constraints before arriving at an optimal solution to the problem. This is a time-consuming process as every time an operating parameter is found to infringe the bounds, the optimization algorithm searches for another optimal solution satisfying the bounds.

This paper is intended to present a simple, yet robust optimization procedure for the design of HF transformer based on core geometry coefficient (defined by McLyman [1993](#page-18-1)) with a constraint imposed on its specific loss. The proposed procedure circumvents the verification of parametric limits for producing an optimal solution as the optimal core geometry (in 5th power of cm) directly brings all the operating parameters like %regulation and temperature rise within preferred limits without compromising on efficiency. Moreover, the proposed procedure is less time consuming than the methods documented in literature as it does not involve verification loops for bounds on operating parameters. Above all, in contrast to other methods where attention need to be paid to avoid saturation effects on magnetic components, the proposed optimization does not have this issue as the core selection is made only after obtaining the optimal core geometry.

The proposed optimization is executed on an isolated half-bridge dc–dc converter with few of the latest bio-inspired algorithms, which are proved to be highly efficient compared with GA. The results of optimization are validated through PowerEsim which unlike other simulation tools is built with practical power supply modules and components from leading manufacturers in the market (Poon [2009\)](#page-19-5).

### <span id="page-3-1"></span>Isolated half bridge DC–DC converter

<span id="page-3-0"></span>A number of dc–dc converter topologies for SST applications have been investigated in the past (Kolar and Ortiz [2014](#page-18-12); Shri [2013\)](#page-19-6) and their relative merits and demerits discussed. Since the primary objective here is the design optimization of HF transformer, a simple half bridge dc–dc converter topology is chosen for unidirectional and Modular SST applications. However, the design optimization can be carried out with any dc–dc converter topology that is deemed appropriate for a particular application.

<span id="page-3-2"></span>[Figure 2](#page-4-0) shows the basic converter schematic and the associated waveforms of a half-bridge isolated dc–dc converter. The element for energy transfer is the leakage inductance of the transformer. The switches  $S_1$  and  $S_2$  are turned on with a phase shift of 180° and both experience a voltage stress equal to that of the input voltage, in contrast to twice the input voltage as in push–pull and forward converters (Vinnikov, Jalakas, and Egorov [2008\)](#page-19-7). Also, the magnetization of the isolation transformer is bidirectional and hence there is no need for a demagnetizing circuit. Other advantages of this converter include less primary turns for the same input voltage and power, lesser winding costs, lower proximity effect losses, no danger of transformer saturation, reduced cost, and its ability to be scaled up to higher power levels.

The apparent power of the transformer in a half bridge converter is calculated as follows:

Secondary apparent power for tapped winding,



<span id="page-4-0"></span>Figure 2. Schematic of isolated half-bridge converter and its associated waveforms.

$$
P_{sy} = (V_o + V_d)I_o * \sqrt{2}
$$
 (1)

where  $V_o$  and  $I_o$  are output voltage and current respectively and  $V_d$  is the diode voltage drop.

Primary apparent power,

$$
P_{py} = \frac{P_{sy}}{\eta} \tag{2}
$$

Thus, total apparent power

$$
P_t = P_{py} + P_{sy} \text{Watts} \tag{3}
$$

The d.c. transfer function of the half bridge converter is derived as

$$
\frac{I_{in}}{I_o} = \frac{V_o}{V_{in}} \approx \frac{1}{2} \cdot \frac{N_s}{N_p} \cdot \frac{2t_{on}}{T}
$$
(4)

### Design optimization

### Procedure

While most of the proposed design methodologies for HF transformers were based on a specified temperature rise, they can also be designed for a given % regulation, " $α$ ". As per definition by (McLyman [1993](#page-18-1)),  $α$  is associated with two coefficients namely, the electrical coefficient " $K_e$ " and the core geometry coefficient " $K_g$ " given by

$$
K_e = 0.145 \left( K_f \right)^2 f^2 B_m^2 \times 10^{-4} \tag{5}
$$

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$$
K_g = \frac{P_t}{2K_e \alpha} \tag{6}
$$

where  $K_f$  is the waveform coefficient,  $P_t$  is the total apparent power in Watts, f is the operating frequency in Hz, and  $B_m$  is the flux density in tesla.

Alternately,  $K_g$  can be expressed as

$$
K_g = \frac{W_a A_c^2 K_u}{MLT} \text{ cm}^5 \tag{7}
$$

where  $W_a$  is the window area in cm<sup>2</sup>,  $A_c$  is the effective core cross-section in  $\text{cm}^2$ ,  $K_u$  is the window utilization factor, and MLT is the mean length of the turn in cm.

From Equations (6) and (7), it is noted that  $K_g$  not only influences the size of the magnetic components but also affects the regulation and copper loss. Thus by optimizing  $K_{\varrho}$ , it is possible to design a transformer, which is more compact and efficient, simultaneously holding the other key design requirements like %regulation, current density in the windings, copper losses, temperature rise etc., within specified bounds.

Referring to Equations (5) and (6), it is clear that  $K_{\sigma}$  is a function of two variables namely,  $f$  and  $B<sub>m</sub>$  with fixed %regulation. Though flux density in the core is actually a function of operating frequency, a good trade-off is needed between these two parameters such that optimum core geometry is achieved. Therefore, while optimizing  $K_{\varrho}$ , frequency and flux density are chosen as the free parameters. The variation of core geometry coefficient with operating frequency and flux density is depicted in [Figure 3](#page-5-0).

The optimization problem in general is stated mathematically as follows:

Find  $X = [X(1) X(2) \dots X(n)]$ , such that  $F = f(X)$  is minimum subject to



<span id="page-5-0"></span>Figure 3. Plot of core geometry coefficient with frequency.

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 $X_{imin} < X(i) < X_{imax}$  where  $i = 1, 2, \dots n$  and  $C_i$   $(X) < 0$ ,  $i = 1, 2, \dots m$ ,

where  $X(1)$ ,  $X(2)$ ,..... $X(n)$  represent the set of independent design variables with  $X_{imin}$  and  $X_{imax}$  as their lower and upper bounds respectively.  $F = f(X)$  is the objective function to be optimized and  $C<sub>i</sub>(X)$  are the design constraints.

Minimize  $K_g$  such that (i)  $f_{min} < f < f_{max}$ (ii)  $B_{mmin} < B_m < f_{mmax}$ 

with the constraint  $W_{pk}$  (f,B<sub>m</sub>) – 0.05\*P<sub>t</sub> <0<sup>†</sup> where  $W_{pk}$  is the specific loss in W/Kg and  $P_t$  is the total apparent power in watts.

† Specific loss is assumed to be limited to 5% of total apparent power.

With f and  $B_m$  chosen as two independent design variables and  $K_g$  as the objective function to be minimized with a constraint imposed on the specific loss of the transformer, the design problem can now be stated as follows.

The design flowchart for the proposed optimization procedure is depicted in [Figure 4.](#page-7-0) The design equations are presented in the Appendix. The inputs to the design problem are power output and voltage levels of the converter. Efficiency and regulation in percentage, waveform coefficient and window utilization factor are chosen to be the fixed parameters. Contrary to the design of low frequency transformer where V/f is held constant to avoid over-fluxing, the operating frequency here is swept across specified limits along with maximum flux density as the choice of core and its dimensions are made only after establishing the optimum core geometry.

Once the best values for the free parameters are found and the optimal value for core geometry coefficient is established using latest bio-inspired algorithms, suitable core material is selected from the core data table corresponding to the optimal value. If there is no precise match for the optimal core geometry coefficient from the core data table, then the core with next higher value for  $K_g$  is chosen to ensure minimal copper loss.

The dimensions of the selected core and their specifications are extracted from the table. With these dimensions and specifications, the current density in the windings, number of turns in the primary and secondary are calculated. The primary and secondary wire areas are then calculated and a wire size with the required wire area is found from the wire table. Subsequently, primary and secondary winding resistances and hence copper losses are calculated. The new values for %regulation and flux density are then updated. The core losses and hence the total losses are calculated followed by the power density and temperature rise.

The design specifications of a single converter module are considered for evaluating the test cases presented in [Table 1](#page-9-0) of this paper. Several such modules



\* Refer Appendix for expressions

<span id="page-7-0"></span>Figure 4. Flowchart for the proposed design optimization of high frequency transformer.

can be connected in parallel at the low voltage side (LVDC link) and in series at the high/medium voltage side (HVDC/MVDC link) as per requirement.

### Algorithms for optimization

<span id="page-8-6"></span><span id="page-8-5"></span>Nature-inspired optimization algorithms are being extensively applied nowadays to solve real and complex engineering design problems (Yang [2010](#page-19-8)). Earlier, GA has been widely applied to solve transformer design optimization problems (Coonrod [1986](#page-17-0); Rama Rao et al. [2004;](#page-19-1) Yadav et al. [2011;](#page-19-9) Versèle, Deblecker, and Lobry [2012](#page-19-10)). However, more recently Artificial Bee Colony (ABC) and PSO algorithms have been employed to solve these problems (Davood, Mehdi, and Jawad [2016\)](#page-18-13).

<span id="page-8-4"></span><span id="page-8-0"></span>In this paper, Particle Swarm Optimization (PSO) algorithm along with three other recently developed algorithms namely, Ant Lion Optimizer (ALO), Dragon Fly Algorithm (DA), and Whale Optimization Algorithm (WOA) are applied to solve the proposed optimization problem and the results are compared with the conventional GA. The proposed optimization procedure is more simple and straight forward than the methods presented in the literature cited above.

<span id="page-8-1"></span>This algorithm emulates the natural hunting behavior of antlions by modeling the interactions between antlions and ants in the trap (Mirjalili [2015](#page-18-14)). The stages involved in hunting process viz., random walk of ants, building traps, entrapment of ants in traps, catching preys, and re-building traps are modeled mathematically. The pseudocode for the algorithm along with a detailed analysis is presented in the reference cited above.

<span id="page-8-3"></span>Dragon fly algorithm This algorithm is inspired by the static (hunting) and dynamic (migration) swarming behavior of dragon flies in nature (Mirjalili, S. [2016b\)](#page-18-15). The collective interaction of dragonflies in traversing, hunting for prey, and evading enemies are modeled as two vital stages of optimization: exploration and exploitation. Random values within specified bounds of variables are used to initialize the position and step vectors of dragon flies which are then updated iteratively until the required criterion is met.

<span id="page-8-2"></span>The social hunting behavior of humpback whales is used to model this algorithm (Mirjalili, S. [2016a\)](#page-18-16). The three steps involved in the hunting process by Whales namely, tracking the prey, encircling the prey, and the bubble-net feeding behavior are modeled mathematically in order to perform optimization.

### Optimization results and discussion

Three test cases are evaluated in support of the proposed optimization procedure and the design specifications for the same are listed in [Table 1](#page-9-0). A single module isolated half-bridge dc–dc converter is chosen for validating the test cases. For modular SST applications, a number of such modules can be cascaded as per requirements. Since the output power of half-bridge converter is limited to 750 W, the test cases are chosen accordingly. However, with higher end dc-dc converters, the power levels can be extended beyond 1 kW. The fixed parameters assumed for all the case studies are common and are presented in [Table 2.](#page-9-1)

The operating frequency, f and the maximum flux density,  $B_m$  which influence the core geometry coefficient (Equations (5) and (6)) are chosen as the free parameters. They are swept over a wide range within specified bounds to find the best optimal value for  $K_{\varrho}$ . The limits for the operating frequency are set between 10 and 120 kHz and that for the maximum flux density between 0.1 and 0.6 T. The upper boundary for flux density is usually set by the saturation flux density of the core material with a safety margin of 10–20% to avoid operation close to saturation. For the case studies considered in this paper, ferrite core is chosen as they have lower core losses (above 20 kHz) and are available in a wide variety of geometric shapes. The maximum value for saturation flux density of ferrite core is 0.45 T. Therefore, the upper limit for  $B_m$  is fixed at 0.6T.

Upon optimization using PSO, ALO, DA, and WOA, the best values for free parameters and the optimal core geometry are established. A comparison of performance of all the algorithms with GA for the three test cases is presented in [Table 3](#page-10-0). All the four nature-inspired algorithms are compared

<b>Table 11 Design specifications of a single conventer module.</b>	Test cases		
Design parameters			Ш
Output power, $P_o$ (W)	250	500	750
Nominal input voltage, $V_{in}$ (V)	100	325	500
Output voltage, $V_o$ (V)	48	100	200
Output current, $I_{\alpha}$ (A)	5.2		3.75

<span id="page-9-0"></span>Table 1. Design specifications of a single converter module

<span id="page-9-1"></span>Table 2. Fixed parameters for optimization.

% Regulation, $\alpha$	0.57
% Efficiency, $\eta$	96
Waveform coefficient, $K_f$	4.0
(for square wave)	
Window utilization factor, $K_{\alpha}$	0.4

		Operating	Maximum flux Core geometry		Average overall	Average no. of		
Test		frequency, f	density, $B_{m\_best}$	coefficient, K <sub>q_opt</sub>	computational	iterations for		
cases		$_{best}$ (kHz) $\,$	(T)	$\text{(cm}^5\text{)}$	time (s)	convergence		
н	GA	74.76	0.1000	0.04496	84.70	27		
	<b>PSO</b>	74.76	0.1000	0.04496	1.46	231		
	DA	74.76	0.1000	0.04496	64.72	278		
	<b>ALO</b>	74.76	0.1000	0.04496	13.25	312		
	WOA	74.76	0.1000	0.04496	5.12	19		
Ш	GA	99.68	0.1088	0.041776	78.80	25		
	<b>PSO</b>	99.99	0.1088	0.041539	1.24	229		
	DA	99.99	0.1088	0.041539	52.24	280		
	<b>ALO</b>	99.99	0.1088	0.041539	11.09	320		
	WOA	100	0.1088	0.041539	4.66	20		
Ш	GA	100	0.12571	0.046257	73.04	25		
	<b>PSO</b>	100	0.12571	0.046257	1.15	212		
	DA	100	0.12571	0.046257	60.31	272		
	<b>ALO</b>	100	0.12571	0.046257	11.55	309		
	WOA	100	0.12571	0.046257	4.84	23		

<span id="page-10-0"></span>Table 3. Comparison of performance of optimization algorithms.

on the basis of identical search agents (equal to 100). The computational speed and the number of iterations for convergence are averaged over 10 successive runs. For the case studies under consideration, it is discerned from the table that all the algorithms return identical optimal solution though they differ in computational speed and convergence. With less number of generations, the optimal value generated by GA is inconsistent in successive runs. However, with an initial population of 200 and increase in number of generations to 1000, GA produces a consistent solution at the cost of increased overall computational time.

The core data pertaining to the optimal value of  $K_g$  are listed in [Table 4](#page-10-1). For all the three test cases, the core having a  $K_g$  value slightly higher than the optimum  $K_{\varrho}$  is selected. This is done to ensure minimal copper loss. The look

	Test	Test Case			Test	Test	Test
Core data	Case I	Ш	<b>Test Case III</b>	Core data	Case I	Case II	Case III
Core material part no.	EE. 43208	DS 43019	RM 42819	Min. core X-sectional area, $A_c$ (cm <sup>2</sup> )	1.299	0.96	0.98
Magnetic path length, MPL (cm)	4.17	4.62	4.4	Total window area, $W_a$ $\text{(cm}^2)$	0.6048	0.7469	0.639
Total core weight, $W_{\text{tfe}}$ (gm)	26	22	23	Area product, $A_n$ (cm <sup>4</sup> )	0.7802	0.717	0.6258
Total weight of copper, $W_{\text{triv}}$ (qm)	19.21	17.32	11.81	Overall surface area of the magnetic component, $A_t$ (cm <sup>2</sup> )	38.22	31.84	29.6
Mean length of the turn, MLT (cm)	8.93	6.52	5.2	Core geometry coefficient, $K_a$ (cm <sup>3</sup> )	0.04507	0.04221	0.04718

<span id="page-10-1"></span>Table 4. Optimal core data.

Transformer	Test	Test	<b>Test Case</b>	Transformer	Test	Test	Test
characteristics	Case I	Case II	Ш	characteristics	Case I	Case II	Case III
Current density, J(A/cm <sup>2</sup> )	569.74	833.89	1228.7	Primary turns, $N_n$	10	31	40
Primary winding resistance, $R_n(\Omega)$	0.0948	0.2719		0.2798 Secondary turns, $N_s$	12	25	41
Secondary winding resistance, $R_s(\Omega)$	0.1138	0.2192	0.2868	Skin depth, $y$ (cm)	0.0242	0.0662	0.0209
Total copper losses, $P_{\text{cut}}(W)$	3.908	6.388	4.9034	Primary wire area, $A_{wn}$ (cm <sup>2</sup> )		0.00516 0.00128	0.00144
Core losses. $P_{fo}$ (W)	0.3757	0.5506	0.8911	Secondary wire area, 0.00596 0.00379 $A_{\text{wfs}}$ (cm <sup>2</sup> )			0.00193
Watt density, $\lambda$ (W/cm <sup>2</sup> )	0.112	0.218	0.196	No. of strands, $S_n$	4	3	2
Regulation, $\alpha$ (%)	1.5	1.25	0.6473	Specific loss, $W_{nk}$ (W/kg)	14.45	25	38.74
Flux density, $B_{mnew}$ (T)	0.1039	0.1081	0.1267	Temperature rise, $\Delta T$ (°C)	7.381	12.78	11.7

<span id="page-11-0"></span>Table 5. Optimal transformer characteristics.

up table for the core data is created with the details obtained from the leading magnetic component suppliers, Magnetics®. [Table 5](#page-11-0) presents the electric, magnetic, and geometric characteristics of the transformer calculated from the optimal core data.

It is inferred from [Table 5](#page-11-0) that the design optimization procedure based on core geometry coefficient proposed in this paper is effective in solving the HF transformer design problem in a simple, yet efficient manner while keeping all the operational parameters like % regulation, temperature rise and system losses within desired limits. Though all the algorithms used for solving the proposed design problem produce the same optimal values for the parameters under consideration, a comparative analysis shows that they differ with respect to speed of convergence, consistency in producing solutions in successive runs, and the speed of computation.

[Figure 5](#page-12-0) shows the convergence of the optimization algorithms plotted for Test Case II. This comparison is based on identical population size and equal number of search agents for all the algorithms except GA. As can be seen from the plot, WOA has high speed of convergence followed by PSO, DA, and ALO. However, referring to [Figure 6\(a](#page-12-1)), it is clear that among the nature-inspired algorithms, DA is more consistent in producing the optimal results in successive runs. Another interesting fact to be noted is that though WOA is quick to converge compared to PSO algorithm, the relative computational time is the least with PSO (less than a couple of seconds) as portrayed in [Figure 6\(b\)](#page-12-1). This is because the computational time per iteration is the least with the PSO algorithm.



<span id="page-12-0"></span>Figure 5. Convergence plot of the optimization algorithms.



<span id="page-12-1"></span>Figure 6. (a) Convergence plot in successive runs. (b) Time plot of convergence in successive runs.

### Design validation and results

The proposed design optimization for HF transformers has been tested using PowerEsim, a web-based result-oriented design tool for power converters and transformers (Poon [2009\)](#page-19-5). Unlike traditional tools, PowerEsim is developed using real-world power supplies and components with due consideration to industrial demands and regulations. As such, it is not a simulation tool but a testing tool used by design engineers and trainees from leading industries across the world to verify and improvise their design.

The design validation of the proposed optimization procedure is carried out for one of the test cases (Test Case II) by selecting a half-bridge converter from the available database in PowerEsim. The implemented schematic and the power circuit component specifications are shown in [Figure 7](#page-13-0) and [Table](#page-14-0) [6,](#page-14-0) respectively. The Mean Time Between Failure (MTBF) analysis for the overall converter circuit is displayed in [Table 7](#page-14-1) and that for the HF transformer is depicted in [Table 8.](#page-14-2) The switching waveforms and performance charts presented in [Figure 8](#page-15-0) reveal the efficiency of the circuit and regulation to be 92.79% and 0.5%, respectively. [Figure 9](#page-16-0) presents the winding arrangement of the HF transformer. From [Figure 10](#page-17-4), it can be seen that the choice of



<span id="page-13-0"></span>Figure 7. Schematic of the half-bridge DC–DC converter implemented in PowerEsim.

<span id="page-14-0"></span>



<span id="page-14-1"></span>Table 7. MTBF analysis of the overall circuit.

At 25 Deg., Standard = MIL-HDBK-217 F Simulated Overall Failure Rate =  $6.264$  failures/10<sup>6</sup> hours Simulated Overall MTBF  $= 159.6$  k hours Simulated Overall Life Time = 76.08 k hours

<span id="page-14-2"></span>Table 8. MTBF analysis of the HF Transformer.

T1	177 uH DS-43019-UG P MAGNETICS transformer final	Failure Rate = $0.1562$ (/10^6 Hrs)
	$(1)$ Bm = 0.121 T	
	$(2)$ Tj = 100 Deg.	
	$(3)$ Wire's Class = 155 Deg. $(F)$	
	$(4)$ Tape's Class = 130 Deg. $(B)$	
	(5) Bobbin's Class = 130 Deg. $(B)$	
	(6) Varnish's Class = 180 Deg. (H)	
	$(7)$ P-S Creepage = Pass	
	$(8)$ Wire Crossed = Pass	

core by PowerEsim tool is a double slab ferrite core with part no. DS43019, similar to the one chosen by the optimization algorithms. However, for the same test case, the choice of the core is HF-5835 with a circuit efficiency as low as 78% using analytical method. This serves as a valid proof for the success of the proposed design optimization procedure for HF transformers in Modular SST applications where regulation and efficiency are considered vital parameters in the design.

### Conclusion

This paper has attempted to present a simple, single-objective design optimization procedure for HF transformers used in modular SST applications. The objective was to optimize the core geometry coefficient with a constraint placed on specific loss such that the design produces a



<span id="page-15-0"></span>Figure 8. (a) Output switching ripple voltage waveform. (b) Input voltage (CH1) and input current (CH2) waveforms. (c) %Efficiency vs. input voltage. (d) Total dissipated losses vs. input voltage. (e) Output voltage regulation. (f) Variation of peak flux density of the transformer with respect to input voltage.

compact and efficient HF transformer with all performance parameters under preferred limits. Four latest nature-inspired algorithms were engaged to accomplish the proposed optimization task and the results compared with GA. It was found that WOA exhibited quick convergence whereas PSO offered best overall performance with respect to convergence and computational time. The proposed optimization procedure was implemented using PowerEsim, a real-time design tool as well and the results were found to be satisfactory.



Figure 9. Winding arrangement of HF transformer.

## <span id="page-16-0"></span>The highlights of the research work are listed below

- This paper is a maiden attempt to optimize the HF transformer based on core geometry (in 5th power of cm) with a constraint imposed on its specific loss keeping regulation and temperature rise within limits in addition to preserving desired efficiency.
- Further, the proposed optimization procedure avoids the need for verification of bounds for parameter values as the optimal value established for core geometry directly brings all the operating parameters within desired limits without compromising on efficiency. Additionally, in contrast to other methods where attention need to be paid to avoid saturation effects on magnetic components, the proposed optimization does not have this issue as the core selection is made only after obtaining the optimal core geometry.
- Three recently developed optimization algorithms namely, Whale Optimization algorithm (WOA), Dragonfly Algorithm (DA), and Ant Lion Optimizer (ALO), which have not been applied to transformer design so far are compared with GA and PSO for their efficacy in solving the optimization problem with respect to various parameters.
- Finally, the optimization results are validated through PowerEsim, a web-based testing platform with huge database of real-time components from leading manufacturers across the globe.



<span id="page-17-4"></span>Figure 10. HF transformer design with PowerEsim.

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### Appendix

(1) Maximum Duty ratio,  $D_{\text{max}} = \frac{1}{T} \left( \frac{T}{2} - t_{dw} \right)$ 

where T is the total time period and  $t_{dw}$  is the dwell time (1  $\mu$ s)

(2) Secondary load power for single winding in Watts,  $P_{ts} = I_o(V_o + V_d)$ 

Secondary load power for tapped winding in Watts,  $P_{ts} = I_o(V_o + V_d) * \sqrt{2}$ 

(3) Total Apparent Power in Watts,  $P_t = P_{ts}(1 + \frac{1}{\eta})$ 

(4) Average primary current in amps,  $I_{pri} = \frac{2P_{ts}}{V_{in}*\eta}$  (for half-bridge converter)

(5) Average primary voltage in Volts,  $V_{pri} = \frac{V_{in}}{2} (2D_{max}) - I_{pri}R_q$ 

where  $R_q$  is the on resistance of transistor in Ohms

(6) Primary turns, 
$$
N_p = \frac{V_{pri} \times 10^4}{K_f B_{m\text{-opt}} f_{opt} A_c}
$$

- (7) Current density in amps/cm<sup>2</sup>,  $J = \frac{P_t \times 10^4}{K_f K_u B_{m\text{-}op} f_{opt} A_p}$
- (8) Primary rms current in amps,  $I_{\text{prms}} = \frac{I_{\text{pri}}}{\sqrt{2D_{\text{max}}}}$
- 

(9) Primary wire area in cm<sup>2</sup>, 
$$
A_{wp} = \frac{I_{prms}}{I}
$$
  
(10) Skin Depth in cm,  $\gamma = \frac{6.62}{\sqrt{f_{opt}}}$ 

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- (11) Wire area in cm<sup>2</sup>,  $A_{wire} = \pi \gamma^2$
- (12) Primary winding resistance in Ohms,  $R_p = MLT(N_p) \left(\frac{\mu \Omega}{cm}\right) \times 10^{-6}$
- (13) Primary copper loss in Watts,  $P_{pcu} = I_{prms}^2 R_p$
- (14) Secondary turns on each side of center tap,  $N_s = \frac{N_p(V_o + V_d)}{V_{pri}}$
- (15) Secondary wire area in cm<sup>2</sup>,  $A_{ws} = \frac{I_o \sqrt{D_{max}}}{J}$
- (16) No. of strands required,  $S_n = \frac{A_{ws}}{A_{wire}(b)}$ , where  $A_{wire}(b)$  is the bare wire area from the wire table
- (17) Secondary winding resistance in ohms,  $R_s = MLT(N_p)\frac{\mu\Omega}{cm}X10^{-6}$
- (18) Secondary copper loss in Watts,  $P_{scu} = I_o^2 R_s$
- (19) Total copper loss in Watts,  $P_{cu} = P_{pcu} + P_{scu}$
- (20) Window utilization factor,  $K_{unew} = \frac{N_p S_n A_{wire}(b) + N_s S_n A_{wire}(b)}{W_a}$
- (21) Regulation in %,  $\alpha_{new} = \frac{P_{cu}}{P_o} X100$
- (22) Flux Density in Tesla,  $B_{mnew} = \frac{V_{pri}X10^4}{K_f f_{opt} A_c N_p}$
- (23) Watts per kilogram,  $WK = 3.18X10^{-4} (f_{opt})^{1.51} (B_{mnew})^{2.747}$
- (24) Core loss in Watts,  $P_{fe} = WK(W_{tfe})X10^{-3}$
- (25) Total Losses in Watts,  $P_{tot} = P_{cu} + P_{fe}$
- (26) Watt density in Watts/cm<sup>2</sup>,  $\lambda = \frac{P_{tot}}{A_t}$

Temperature rise in °C,  $\Delta T = 450(\lambda)^{0.826}$